Cost Competition, Fragmentation and Globalization

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Abstract
This paper proposes a model in which the removal of barriers to trade and factor mobility is associated with endogenous fragmentation of the value-added chain. Fragmentation is the outcome of cost competition – the profit-maximizing choice of cost structure by monopolistically competitive firms. An expansion of the integrated trading area can induce globalization not only in the horizontal dimension associated with love-of-variety preferences, but also vertically as firms vary specialization of production stages. While increased trade is likely to induce fragmentation when the number of firms is fixed, free entry can either reverse or intensify this result.

JEL-Classification: F10, L23, O33

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1. Introduction

At the outset of the new millennium, usage of the term "globalization" has become so extensive that it risks trivialization. While a precise definition of globalization remains elusive in both academic and popular discussion, one defining aspect must be the leap in economic integration of the world's economies over the last few decades; in the OECD, the ratio of international trade to value added rose from 24.6 percent in 1960 to 42.7 percent in 1996 (OECD (1998)). Yet many observers have noted that on this metric, the world is no more integrated today than it was at the turn of the last century; one frequently reads of "globalization cycles" in economic history.¹

The causes of globalization today appear to be fundamentally different, however, to those at the dawn of the last century. We are witnessing a wave of fundamental developments which are changing ways that nations interact economically with each other. Mega-mergers and cross-border firm linkages have intensified trade in intermediate goods. An especially impressive development has been the rise in outsourcing, which allows firms to extend activities across national boundaries and tailor manufacturing strategies to idiosyncratic attributes of local production sites. The word "fragmentation" has been used to characterize these developments (e.g. Deardorff (1998); Jones/Kierzkowski (1990; 1997; 1999); Feenstra (1998); Kierzkowski (1998)).

At the same time, a large and growing body of research confirms that the intensification of trade is best characterized as vertical rather than horizontal. Krugman (1995) points out that export to GDP ratios exceeding 30 percent can only be explained by reference to vertically linked trade. This applies in particular to countries with total trade exposure exceeding total economy value added. At the level of the OECD, Yeats (1998) estimates that the share of trade in parts and components within the SITC 7 category (i.e. machinery and transportation equipment) increased by 4 percentage points between 1978-95 and currently stands at more

than 30 percent; he considers these numbers as representative for manufactured goods in general. Yeats' estimates, based on recent revisions of trade statistics, are in line with estimates by Campa/Goldberg (1997), who examined input-output data of 20 industries on the 2-digit SIC level from the UK, the US and Canada and found that in almost all industries the imported share of inputs (in total inputs) rose in the period 1975-95. Looking at the share of imported inputs in exports, Hummels/Rapoport/Yi (1998) found similar evidence.²

This aspect of globalization is the focus of our paper. In particular, we ask the question: under what circumstances and to what extent can the opening up of trade itself account for the increasing fragmentation of world economic relations? In the model we propose below, fragmentation is driven by Smithian division of labor and pure economies of scale, and results from cost competition among firms. To highlight these effects, we exclude any exogenous variation in technology from our analysis.³

Globalization of this sort can differ considerably from that derived in models of horizontal trade alone. North-South models of the HOS or Ricardian type are often difficult to reconcile with product and labor market developments in industrialized countries.⁴ Endogenous changes in production methods, rather than low wage competition, are responsible for an increase in the relative demand for skill in our model. For further emphasis, we focus our attention on fragmentation in an integrated economy, bypassing for the moment physical trade flows to emphasize the endogeneity of production and cost structures.

The paper is organized as follows. Section 2 offers a brief review of the literature on fragmentation and trade. Section 3 proposes our model of endogenous fragmentation in an

² The same pattern of increases in outsourcing and intra-industry trade in components is also displayed by area and industry studies (Ng/Yeats (1999); Jones/Kierzkowski (1999)).
³ For a discussion of globalization related to intermediates production and outsourcing driven by factor proportions and Ricardian differences, see Sanyal/Jones (1982), Sanyal (1983), Feenstra/Hanson (1996a,b), and Deardorff (1998)); outsourcing related to factor intensities of multinationals is discussed by Slaughter (1999)).
⁴ It has proven difficult to explain recent labor market developments in OECD countries. An overwhelming majority of studies from the perspective of both trade volumes (Sachs/Shatz (1996), Cooper (1994), but see also Wood (1994)) and prices (Lücke (1998)) have found little evidence of globalization along HOS-lines. The predicted pattern of substitution from skilled towards unskilled labor stands in contrast to actual developments: in particular in the US, the unskilled-skilled ratio fell in virtually all industries (Berman/Bound/Machin (1998)).
integrated economy and illustrates the central role of the labor market in determining the resource cost of fragmentation, which we interpret as the production of business services. As the impact differs depending on whether one adopts a short-run or a long-run perspective we will distinguish between two model variants: one with a fixed number of firms and another with free entry. Section 4 reinterprets the model as a benchmark integrated economy and presents the central comparative statics results linking the size of the trading area to globalization as we understand it in this paper. Because the model allows for trade in differentiated final goods, it permits the useful distinction between globalization in horizontal and vertical dimensions. An important finding is that while increased trade is likely to induce technological change in the form of fragmentation in the short run (when the number of firms is fixed) free entry can either reverse or intensify this result. Section 5 concludes.

2. A Review of the Theoretical and Empirical Literature

A number of contributions have featured the fragmentation of production processes as a concomitant phenomenon of globalization (see Francois (1990a,b), Jones/Kierzkowski (1990; 1997; 1999)). In general, these models abstract from opportunity costs of resources employed in managing the fragmented value added chain. Jones/Kierzkowski (1990) emphasize the role of producer services in the fragmentation of production process without a formal model. In Jones/Kierzkowski (1997), specialization in intermediates is driven by stages of production and endowments (see also Feenstra/Hanson (1996a,b)). Drawing on the examples of the photo-imaging and pharmaceutical industries, Jones/Kierzkowski (1999) describe how fragmentation allows sharing of production blocks across various industries and how indivisibilities and economies of scope increase complementarities between horizontal linkages among industries and vertical specialization.

Francois (1990a) explicitly accounts for services and employs a family of production functions as developed by Edwards/Starr (1987) to display economies of scale as
fragmentation is increased, but features a single (homogeneous) labor market. Most importantly, he stresses the endogeneity of the elasticity of substitution in demand along the lines of Lancaster (1979), so that demand and market size drive fragmentation (see also Dluhosch (2000)). In a related paper, Francois (1990b) assumes that services are produced with high skilled labor only while direct production uses unskilled labor but retains Lancaster preferences in demand, which he considers crucial for fragmentation (see Francois (1990b:723, fn. 6)).

Another salient aspect of models studying horizontal and vertical trade as globalization is the assumption of Dixit-Stiglitz (1977) "love-of-variety" preferences (Krugman (1980; 1981), Helpman (1981)). In principle, trade in these models is driven by the demand-side as well. Because consumers prefer greater variety of goods, larger markets sustain larger numbers of businesses; in equilibrium, competition occurs via the number of firms, not via the scale of production. Love of variety in intermediates may feature increases in productivity and scale in final goods production, but in the end this process is demand-driven as well. Some examples of this approach are Markusen (1989); Feenstra/Markusen/Zeile (1992); Feenstra/Markusen (1994); Krugman/Venables (1995); Ethier (1982) and Romer (1987).

Our model shifts focus from demand to supply as an alternative engine of globalization. We model fragmentation as an endogenous choice of cost-competitive firms in a general equilibrium setting with two factors of production. The scale of production of individual firms changes endogenously, while the production process becomes more fragmented and global sourcing increases. In our framework, labor markets turn out to be crucial for integration-driven fragmentation. Business services produced with skilled labor are necessary for managing global production and therefore determine the equilibrium extent of fragmentation. Explicit modeling of the supply side of fragmentation is a central contribution of our model.

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5 Krugman (1981) addresses this issue by assuming differentiated products segmented on the demand-side along industry groups.
6 On labor market implications in particular see also Matusz (1996).
3. Cost Competition and Technological Choice under Monopolistic Competition in the Closed Economy

3.1. Household Preferences and Demand

We consider an economy populated by identical households which consume a large number \( N \) of differentiated, manufactured goods in quantities \( x_i \) as well as a homogeneous consumption service good \( x_0 \), which serves as the model’s numeraire. Preferences over manufactured goods are described by the standard Dixit-Stiglitz (1977) symmetric CES function, which is nested in turn in Cobb-Douglas utility with expenditure shares of \( \mu \) and \((1-\mu)\) for manufactured goods and consumer services, respectively. Given income \( Y \), utility maximization gives rise to the familiar demand functions

\[
x_i = \left( \sum_{j=1}^{N} p_j^{-\eta} \right)^{-1} \mu Y p_i^{-\eta} \quad \text{for } i=1,...,N
\]

\[
x_0 = (1-\mu)Y,
\]

so that for \( N \) large, the elasticity of demand for manufactured goods is approximately \( \eta \).

3.2. Manufactured Goods and Technology of Cost Reduction

Each of the \( N \) differentiated manufactured goods is produced by a single monopolistically competitive firm. A central innovation in this paper is that the supplier of each variety can influence its own costs by choosing the length or roundaboutness of production, and thereby the degree of specialization of individual production stages. This aspect of technology is summarized by a positive real number \( z \). Since we allow for noninteger values, it is best to think of \( z \) as an index of fragmentation or specialization of stages in the value added chain.\(^7\) A small increase in fragmentation or specialization \( dz \) (or an incremental lengthening of the

\(^7\) Since our model refers primarily to industry or economy-wide phenomena and not to the firm, ignoring the integer problem should not be an important issue.
production process) reduces direct production costs, but also generates additional fixed costs \( p_z dz \), so \( p_z \) is the cost of adding and managing an intermediate production stage.

Direct production costs of \( x \) units of the manufactured good consist of direct fixed costs \( F > 0 \), and direct variable costs \( v(z)x \) which are subadditive over the \( z \) stages, so that total direct production costs for a representative firm are given by \( F + v(z)x \), with \( v' < 0, v'' > 0 \). This formulation is consistent with Adam Smith's (1776) idea that the size of the market determines the extent to which specialization increases productivity and reduce variable costs. To facilitate analysis, we assume an isoelastic form \( v(z) = \frac{v}{z^\gamma} \) with \( 0 < \gamma < \frac{1}{(\eta-1)} \).

Total production costs for firm \( i \) are then given by

\[
F + \frac{v}{z_i^\gamma} x_i + p_z z_i. \tag{2}
\]

3.3. Optimal Firm Behavior and Partial Product Market Equilibrium

Because they deliver fundamentally different results, we distinguish two cases of partial product market equilibrium. In the first case, the market for manufactures is served by a fixed number of established firms in what might be regarded as a short-run analysis. The second case adopts a long-run perspective and assumes free entry, so that all economic profits are competed away. In this section we derive the generic partial product market equilibrium which we later specialize to the two different market situations.

Profits of the representative firm in manufacturing can be written as the difference between total revenues and total production costs:

\[
p_z x_i - \left[ F + \frac{v}{z_i^\gamma} x_i + p_z z_i \right] \tag{3}
\]

---

8. Fixed costs might also be affected by choice of \( z \), but in the end it is relative cost differences that are crucial and these can be captured by focusing on variable costs.

9. This implies that marginal costs at \( z=0 \) are infinite, so demand for \( z \) will be strictly positive. The explicit bounds on \( \gamma \) are necessary to prevent fragmentation from being "too efficient" in cost reduction.
Since firms produce differentiated goods with identical technologies, describing (partial)
product market equilibrium without entry is straightforward. The $i^{th}$ firm maximizes profit
given by (3) by its choice of output level $x_i$ and cost reduction $z_i$, taking $p_z$ and its output
demand curve (1a) as given. Combining the first order conditions (not shown) with the
symmetry of manufactured goods in utility and production, we have $p_i=p_j=p$, $x_i=x_j=x$ and
$z_i=z_j=z$ for all firms $i$ and $j$. For a given $N$, it follows that

\[ x = \left( \frac{(\eta-1)\mu Y}{\eta N} \right)^{\frac{1}{\gamma}} \left( \frac{\gamma}{p_z} \right)^{\frac{1}{\gamma}} \]  

(4a)

\[ p = \left( \frac{\eta}{\eta-1} \right)^{\frac{1}{\gamma}} \left( \frac{p_z N}{\eta Y} \right)^{\frac{1}{\gamma}} \]  

(4b)

\[ z = \frac{(\eta-1)\mu Y}{\eta N p_z} . \]  

(4c)

Equations (4a-c) convey a number of implications of cost competition in partial equilibrium:

- production fragmentation $z$ depends negatively on the costs of fragmentation, $p_z$ and
  positively on total income $Y$;

- the price of manufactured output $p$ (in terms of consumer services) depends positively on
  $p_z$ and negatively on $Y$, while marginal costs are now endogenous;

- the scale of the firm $x$ depends both on aggregate income $Y$ as well as incentives and
  ability of firms to reduce costs ($p_z$ relative to $Y$).

To enforce consistency of the cost function with a primal problem in two factors of
production, we assume that direct production costs of manufacturing firms represent
payments for the output of a perfectly competitive intermediate sector which employs skilled
labor $H_P$ and unskilled labor $L_P$ using the constant returns production function $f(H_P,L_P)$ and
sells its output at price $p_C$.\textsuperscript{10}
3.4. Business Services

The partial equilibrium analysis of the last section treated the price of business services \( p_z \) and aggregate income \( Y \) as given. If \( Z (=Nz) \) is produced by profit-maximizing firms using resources with value in alternative uses, this is assumption is clearly vulnerable.\(^{11}\) To complete the model, it is necessary to incorporate explicitly the supply of labor to business services and the other two productive sectors, consumer services and manufacturing production. In this way we can pin down the equilibrium aggregate supply of business services \( Z \) and its relative price \( p_z \), and by extension, the extent of firm-level fragmentation \( z \).

Irrespective of whether they involve geographical reallocation of industries, the fragmentation of production absorbs resources in the form of additional coordination and communication capacities, as well as middle management, sales and legal personnel. These resource requirements are modeled explicitly as a demand for business services produced with skilled labor. It is here that the link between fragmentation and the labor market is established.\(^{12}\) By suitable normalization, the length of the production process \( z \) of the representative firm gives rise to an equal demand for business services, which can be interpreted as an intermediate input to manufacturing. Economy-wide demand for business services \( Z \) is thus given by \( Nz \):

\[
Z = Nz. \tag{5}
\]

Business services are supplied in quantity \( Z \) by perfectly competitive, profit-maximizing firms using skilled labor \( H_s \) and the constant returns production function

\(^{10}\) We assume that \( f \) has the usual properties; that is, \( f_{ih} \cdot f_{il} > 0; f_{ihh}, f_{ill} < 0; f_{ili} > 0; \) and \( f_{ihh} \cdot f_{ill} -(f_{ili})^2 = 0 \).

\(^{11}\) In the original work of Kennedy (1964), Samuelson (1965) and von Weizsäcker on factor bias of technological change, these resource requirements were not explicitly modeled.

\(^{12}\) Some of these channels have been stressed by Harris (1995). Becker/Murphy (1992) point out that the division of labor is more often determined by costs of coordinating the various activities rather than size of the market. Our formulation is consistent with the fact that average compensation in business services is higher than in the overall economy while skill premia are on the rise (OECD 1999). The referee has pointed out that \( z \) might simply represent firm investments in specific human capital. This alternative interpretation would fail to account for the strong concentration of recent employment growth in administration and management observed in OECD countries (Burda/Dluhosch (1999)).
with $A>1$. The market price of business services in terms of the numeraire $p_z$ is taken as given, so the derived demand for labor in this sector is infinitely elastic at $Ap_z$ which will be the equilibrium wage in the economy for skilled labor.

3.5. Consumer Services

Competitive firms produce consumer services using unskilled labor with a constant returns technology

$$x_0 = L_S$$

so labor demand in this sector is infinite elastic at real product wage of unity. As with business services, the assumption that consumer services are produced with low-skilled labor is driven by the fact that compensation in that sector is generally below average (OECD (1999)).

3.6. Labor Market Equilibrium

Households supply labor inelastically in two forms, skilled $H$ and unskilled $L$. Labor markets are segmented by skill level; they are assumed to clear, and mobility between alternative uses (sectors) is costless; the demand curve for each type of labor in each sector is the "supply price" to the other. It follows that two equilibrium conditions are the equality of wage and value marginal product for both types of labor:

$$1 = p_c f_L (H - H_S, L - L_S)$$

$$Ap_z = p_c f_H (H - H_S, L - L_S),$$

where $p_c$ is the market price of the intermediate input which constitute the direct costs to the manufacturing sector.
3.7. Closing the Model in the Short Run: No Entry

Since the general equilibrium impact of the size of the trading area depends on whether we assume free entry of firms or not, we distinguish two situations: one in which we allow firms to make profits, and another in which a zero profit condition is imposed. We now characterize first the equilibrium outcome when the number of firms is fixed at $\bar{N}$.

To close the model we require two output market equilibrium conditions. The first concerns the market for business services ($Z$), equating demand of $\bar{N}$ firms given by (4c) and (5) with total market supply given by (6):

$$\frac{(\eta-1)\frac{\mu\gamma}{\eta\psi}}{\eta\psi} = AH_S$$

(10)

The second equilibrium condition is that the value of demand for direct cost input of manufacturing firms must equal production:

$$\bar{N}[F + \bar{v}z\gamma x] = p_C f(\bar{H} - H_S, L - L_S)$$

(11)

With the number of firms fixed at $\bar{N}$, (1b), (4a), (4b), (4c), (7) (8) (9) (10) (11) are nine equations in $x_0$, $x$, $z$, $p$, $p_o$, $p_C$, $H_o$, $L_o$, and $Y$. By virtue of its recursive structure, the model can be reduced to the following system of three equations in $L_o$, $H_o$, and $p_o$:

$$p_o A = \frac{f_H}{f_L}$$

(12)

$$\frac{L_o}{(1-\mu)} = \frac{\eta}{(\eta-1)\frac{\mu}{\eta} p_o AH_S}$$

(13)

$$\bar{NF} + \frac{(\eta-1)\frac{\mu}{\eta(1-\mu)}}{L_o} = \frac{f}{f_L}$$

(14)

Since the right hand side of equation (14) represents total direct costs in manufacturing valued in terms of the numeraire, the left hand side can be interpreted as its allocation into fixed $\bar{NF}$ and equilibrium variable $\frac{(\eta-1)\frac{\mu}{\eta(1-\mu)}}{L_o}$ components.
3.8. Closing the Model in the Long Run: Free Entry

In case of free entry, an additional zero profit condition is imposed on the system (4a-c). Profits are driven to zero by endogenous variation in product variety and the number of firms, both given by $N$. Setting (3) to zero and substituting (4) yields the following relationship between product variety $N$ and income $Y$:

$$N = \frac{(1 - \gamma(\eta - 1))\mu Y}{\eta F}\text{.}$$  \hspace{1cm} (15)

It is now clear that in order for positive equilibrium market size, equation (15) requires $0 < \gamma(\eta - 1) < 1$, which we have already assumed above. Combining (15) with (4a-c) yields the following symmetric product market equilibrium conditions with free entry:

$$x = \left(\frac{F(\eta - 1)}{(1 - \gamma(\eta - 1))} \right)^{\gamma/\eta} \left(\frac{\gamma}{p_z}\right)^{\gamma/\eta} / \gamma$$  \hspace{1cm} (16a)

$$p = \left(\frac{\eta}{\eta - 1}\right)^{\gamma/\eta} \left(\frac{(1 - \gamma(\eta - 1))p_z}{\gamma F}\right)^{\gamma/\eta}$$  \hspace{1cm} (16b)

$$z = \frac{(\eta - 1)pF}{(1 - \gamma(\eta - 1))p_z}\text{.}$$  \hspace{1cm} (16c)

With free entry, partial product market equilibrium can be characterized exclusively in terms of $p_z$. Note now that:

- due to free entry and replication, aggregate income $Y$ as well as the fraction spent on manufactures by consumers, $\mu$, are irrelevant for the partial product market outcome;
- in contrast to Dixit/Stiglitz (1977) and Krugman (1980, 1981), the equilibrium scale of the firm $x$ is not constant under free entry, but depends on the cost of fragmentation ($p_z$). From (16a), $x$ becomes constant as $\gamma$ goes to 0, as in Krugman (1980, 1981);

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13 Again, we ignore integer issues here.
- from (16b), the equilibrium price manufactured output \( p \) (in terms of consumer services) depends positively on \( p_z \) only. As \( \gamma \) approaches zero, the markup converges to the familiar Lerner index of monopoly power (see Lerner (1934));
- an increase in market power of the representative firm (a decline in \( \eta \)) reduces both the output of firms and expenditures on cost reduction unambiguously.\(^\text{14}\)
- the share of fixed and variable costs in direct costs at the optimum is constant.\(^\text{15}\)

Under free entry, the model consists of the same system as that without entry plus the zero profit condition (15). As before, it can be reduced to a system of three equations in three unknowns \( L_s, H_s, \) and \( p_Z \):

\[
p_z A = \frac{f_H}{f_L} \tag{17}
\]

\[
\frac{(\eta - 1)\mu}{\eta(1 - \mu)} = \frac{p_z A H_s}{L_s} \tag{18}
\]

\[
\frac{[\eta - \gamma(\eta - 1)]\mu}{\eta(1 - \mu)} = \frac{f}{L_s f L} \tag{19}
\]

4. International Trade, Fragmentation and Globalization

4.1. Interpreting the Model in Terms of Trade and Globalization

Until now the model could be thought of as a closed economy in which fragmentation of production occurred only in the home country. However, two important aspects of international trade can be captured. Like conventional trade approaches, the current model predicts that an enlargement of the trading area can have real effects on production patterns.

\(^\text{14}\) To see this, note that

\[
\frac{dz/d\eta}{\eta} = \frac{\gamma F}{[1 - \gamma(\eta - 1)] + (\eta - 1)\gamma F} \geq \frac{\gamma F}{[1 - \gamma(\eta - 1)] p_z} > 0.
\]

\(^\text{15}\) Inserting optimal behavior (16a) and (16c) in \( F + vz \gamma x \) yields \( \frac{\eta - \gamma(\eta - 1)}{1 - \gamma(\eta - 1)} F. \)
Generally, two nations that open up to international trade and produce as an integrated economy could potentially produce twice as many differentiated products goods or even more; horizontal globalization means that the representative household can augment the variety of its consumption basket via purchases of "foreign" goods.\textsuperscript{16} Trade in conventional models with differentiated goods has been used to explore the effects of opening up closed economies of similar development to trade (e.g. Brander (1981), Krugman (1980, 1981)). Since Dixit-Stiglitz preferences presume a boundless appetite for variety, the number of available goods will increase if determined endogenously.

Yet as pointed out in the introduction, a dramatic increase in trade in intermediate inputs and a secular fragmentation of the value-added process, associated with "global sourcing," has proceeded at the same if not at a faster pace than world trade (Campa/Goldberg (1997)). Therein lies the role of the cost reduction technology: increasing intra-industry trade increases incentives of firms to achieve higher volumes by investing in production sites and thereby economizing on variable costs; according to (5), the equilibrium effect on $N$ is potentially indeterminate if profits are competed away because of entry. In our framework, vertical globalization will reflect the process by which the fragmentation of production is achieved within and across international boundaries. The distinction between deepening (vertical) and broadening (horizontal) globalization is an important one.\textsuperscript{17}

There are at least two ways to relate these two dimensions of globalization to trade. One is to employ the Samuelsonian metaphor (Samuelson (1949)) and ignore national boundaries; it would be sufficient to study the effects of exogenous changes in factor endowments on the integrated economy.\textsuperscript{18} The next step would be to model trade explicitly and ask whether the

\textsuperscript{16} Admitting only intraindustry specialization, our framework is somewhat special; it is explicitly rigged to produce answers that are not related to the factor proportions model of trade, which has not fared well in explaining North-North trade in any case (Lücke (1998)).

\textsuperscript{17}This paper thus extends the analysis of Krugman's (1980), who seems to be arguing that scale effects are impossible in a constant elasticity world (p. 200). In our model, optimal scale can differ across different zero profit equilibria as firms “economize” on variable costs to varying degrees.

\textsuperscript{18}This is in line with the widely-held view that intensifying trade has resulted from declining trade barriers (see Wood (1994)).
integrated economy can be replicated as has been done in the intra-industry trade literature (see Helpman's (1984) paper in the Handbook of International Trade). If some goods are not traded, however (i.e., services), there is no guarantee that the integrated economy can be achieved. In this paper we restrict our analysis to the first approach.

Our model predicts that an enlargement of the trading area – achieved for example by the removal of barriers to trade and mobility between countries – will have two effects. First, a horizontal effect reflected in the number of firms in manufacturing \( N \) of the traditional intra-industry sort. Second, however, an enlarged market for a given trading region, *ceteris paribus*, will increase incentives for individual firms to economize on variable costs by outsourcing or fragmenting the production process \( z \). In this sense, an enlarged market associated with trade drives an endogenous evolution of technology, which in turn affects the international division of labor.\(^{19} \) There is, however, no reason to believe *a priori* that increased trade will necessarily lead to more fragmentation. In fact, our model suggests that while fragmentation increases in the short run, it could be reversed in the long run as firms face competition from newly entering firms. In the next section we explore formally in a comparative statics analysis the conditions under which a larger trading area in the integrated economy will increase the degree of fragmentation of the representative firm, \( z \).

4.2. The Effects of an Enlarged Trading Area: No Entry

As emphasized in Section 3.3, a variable of central importance to the model economy is the price of business services \( p_Z \) – the market price of fragmentation. From equations (4a)-(4c), it determines the degree of vertical versus horizontal globalization via its influence on the demand for fragmentation at the individual firm level \( z \), the relative price of manufactured goods \( p \) and the optimal scale \( x \). In general equilibrium, \( p_Z \) will be influenced by the technology of business services as well as the opportunity cost of skilled

\(^{19} \) This possibility has been discussed in the context of outsourcing by Feenstra (1998).
labor in the manufacturing sector, and will thus depend on the elasticity of substitution between skilled and unskilled labor as well as employment opportunities of unskilled labor. Only with the help of formal comparative statics analysis is it possible to show under which conditions globalization of production related to fragmentation increases due to an increase in the size of the trading area only.

We model the enlargement of markets as an exogenous increase in factors of production: \( \dot{H} > 0, \dot{L} = \omega \dot{H} \) with \( \omega \geq 0 \). The case of \( \omega = 1 \) corresponds to an equiproportional increase in both factors; i.e. a simple up- or downscaling of the absolute size of the economy.

In what follows, we identify conditions under which cost competition leads to vertical globalization of production – an increase in the number of production sites for the representative firm (\( dz > 0 \)), rather than merely an increase in the number of products (\( dN > 0 \)). Naturally, an increase in fragmentation for the aggregate economy is possible either via an increase in firm-level fragmentation or an increase in the number of firms.

Using standard notation from Jones (1965), we let \( \lambda_{ij} \) be the share of labor input \( i \in \{ \text{high-skilled (H), low-skilled (L)} \} \) employed in \( j \in \{ \text{production (P), services (S)} \} \), let \( \Theta_j \) be the elasticity of \( f \) with respect to \( i \) (with \( \Theta_{HP} + \Theta_{LP} = 1 \)) and the local elasticity of substitution of \( f \) as \( \sigma \equiv \frac{f_H f_H}{f_H f} \). Log-differentiation of (12), (13), and (14) yields the following system of three equations in \( \dot{L}_S \), \( \dot{H}_S \), and \( \dot{p}_Z \) for a given number of firms in manufacturing:\(^{20}\)

\[
\begin{pmatrix}
-\frac{(1-\lambda_{LP})}{\lambda_{LP}} & \frac{(1-\lambda_{HP})}{\lambda_{HP}} & -\sigma \\
S\sigma + \frac{(1-\lambda_{LP})}{\lambda_{LP}} \Theta_{HP} (1-\Theta_{HP}) & -1 & -1 \\
S\sigma + \frac{(1-\lambda_{LP})}{\lambda_{LP}} \Theta_{HP} (1-\Theta_{HP}) & -1 & -1 \\
\end{pmatrix}
\begin{pmatrix}
\dot{L}_S \\
\dot{H}_S \\
\dot{p}_Z \\
\end{pmatrix}
\]

\[ (20) \]

\(^{20}\) Details on these and other derivations in this paper can be found in an appendix available from the authors.
\[
\begin{bmatrix}
\sigma \\
1 \\
0
\end{bmatrix} \hat{A} + \\
\begin{bmatrix}
-\left(\frac{\omega \lambda_{x_H} - \lambda_{x_L}}{\lambda_{x_H} \lambda_{x_H}} \right) \\
\lambda_{x_L} \theta_{H_P} (\sigma - 1) + \left(1 - \theta_{H_P}\right) (1 - \lambda_{x_H}) \lambda_{x_H} \\
0
\end{bmatrix} \hat{H}
\]

where carats (e.g. \( \hat{x} \) for \( dx/dx \)) denotes percentage changes and \( s = \frac{(\eta - 1)\eta L_S}{\eta (1 - \mu) + NF} \) stands for the equilibrium fraction of variable costs in total direct costs in manufacturing.

Equation (20) expresses the evolution of three central variables – unskilled employment in consumer services, skilled employment in business services and the price of business services in terms of the numeraire – as a function of a small change in the size of the market.

To repeat, the skill composition of this market enlargement is parameterized by \( \omega \) if \( \omega = 0 \), the trading area experiences an increase of skilled labor only; \( \omega = 1 \) corresponds to the case of an equiproportional increase in both factor endowments; \( \omega > 1 \) denotes the case in which growth in the supply of unskilled labor exceeds that of skilled workers.

Solution of the model involves a straightforward application of Cramer's Rule to (20). It is necessary to establish the sign of the determinant \( \Delta_N \), which is given by

\[
\Delta_N = -\frac{\sigma}{\lambda_{x_H} \lambda_{x_H}} \left\{ (1 - \lambda_{x_H})(1 - \lambda_{x_H}) + \sigma \theta_{H_P} (1 - \lambda_{x_H}) \lambda_{x_H} + (S - \theta_{H_P})(1 - \lambda_{x_H}) \lambda_{x_H} \right\}
\]

A sufficient condition for \( \Delta_N < 0 \) is that the share of variable costs in direct manufacturing is sufficiently high, or \( S > \theta_{H_P} \). Another is \( (\sigma - 1)(\lambda_{x_H} - \lambda_{x_H}) \geq 0 \), which is fulfilled if direct manufacturing is skill-intensive and substitution between skilled and unskilled labor is limited. The necessary and sufficient condition for \( \Delta_N < 0 \) can be expressed as

\[
S > \frac{\theta_{H_P} (\lambda_{x_H} - \lambda_{x_H})(\sigma - 1) - (1 - \lambda_{x_H}) (1 - \lambda_{x_H}) + \lambda_{x_H} \sigma}{(1 - \lambda_{x_H}) \lambda_{x_H} + \sigma \lambda_{x_H} \lambda_{x_H}}
\]

which is likely to hold for conventional parameter values, even for small \( \sigma \). The intuition is that incentives to substitute fixed for variable costs as measured by \( S \) (the share of variable in
total costs) must be sufficiently large. For the rest of the paper, we will assume that this condition holds.

**Skilled and Unskilled Employment in Services**

The response of employment in the two service sectors to an expansion of size of the trading area (as parametrized by the endowment of inelastically supplied labor) is of central importance in this model. Equilibrium fragmentation will depend on how labor markets allocate labor to alternative uses; in particular, on how much high skilled labor is employed by the business services sector.

The solution of (20) yields the following log differential change in employment of low-skilled labor in services ($\hat{L}_S$):

$$\hat{L}_S = -\omega (1 - \lambda_{HP}) + \left[\lambda_{PL} - \lambda_{HP}\right] (\sigma - 1) + \left[\theta_{HP} + \left(1 - \theta_{HP}\right) \sigma\right] \omega \lambda_{HP} \frac{\hat{s}}{\sigma H}$$

so a sufficient condition for positive $\hat{L}_S$ is $\sigma \geq 1$. The necessary and sufficient condition is

$$\sigma > 1 - \frac{\omega}{\lambda_{PL} \theta_{HP} + \omega \lambda_{HP} (1 - \theta_{HP})}$$

which is met for plausibly small $\sigma$ and $\omega$. For example, any $\omega$ fulfilling $\omega > \frac{\lambda_{PL} \theta_{HP}}{1 - \lambda_{HP} (1 - \theta_{HP})}$ will work for all admissible values of $\sigma$.

The logarithmic change in high skilled employment in business services is given by

$$\hat{H}_S = -\lambda_{PL} \theta_{HP} (\sigma - 1) + S \left[\left(1 - \theta_{HP}\right) \sigma + \theta_{HP} - \omega \lambda_{HP} + \left(1 - \lambda_{PL}\right) \frac{\hat{s}}{\sigma H} \right]$$

$$= \frac{-\sigma}{\lambda_{PL} \lambda_{HP} \lambda_N} \left[\left(\lambda_{PL} - \lambda_{HP}\right) \sigma + \lambda_{PL} \sigma - (1 - \theta_{HP}) \sigma - \theta_{HP}\right]$$

(24)

The necessary and sufficient condition on $\sigma$ for positive $\hat{H}_S$ is
which is met even for some large values of $\omega$, i.e. for some $\omega > \frac{\lambda_{LP}}{\lambda_{HLP}}$.

To summarize, the model predicts a bimodal increase in both high- and low-skill services employment and is thus consistent with current developments in OECD-countries. A requirement for this result is a sufficiently large elasticity of substitution between skilled and unskilled labor in the manufacturing sector, with the critical value being strictly less than unity, the Cobb-Douglas case.

**Fragmentation and Market Price of Business Services**

With the number of firms fixed, the extent of firm-level fragmentation (vertical globalization) can be derived directly from aggregate fragmentation ($z = Z / \bar{N}$). Since $Z = AH_S$, firm-level fragmentation increases in response to an expansion of the trading area as long as $H_S$ increases, the conditions for which were established above. Equivalently, inspection of (4c) reveals that the necessary and sufficient condition for firm-level vertical globalization is $\hat{Y} > \hat{p}_z$ or, since $L_S = (1-\mu)Y$, $\hat{L}_S > \hat{p}_z$. Thus, it is possible in the short run for the price of fragmentation to rise even while fragmentation at the level of the firm is increasing. The comparative statics result for $\hat{p}_z$ is

$$\hat{p}_z = -\frac{(\omega \lambda_{HLP} - \lambda_{LP})S}{\lambda_{LP} \lambda_{HLP} \Delta_N} \frac{(1 - \lambda_{LP}) + \omega (1 - \lambda_{HLP})}{\sigma H}$$

(27)

To sign (27) unambiguously, it is convenient to express parameter restrictions in terms of $\omega$. With $\Delta_N < 0$, the price of fragmentation will rise in short-run equilibrium without entry if and only if

$$\omega > \frac{1 - \lambda_{LP}(1 - S)}{1 - \lambda_{HLP}(1 - S)}$$

(28)
It is worth remarking that if both conditions (26) and (28) are met, an increase in the trading area not only leads to an increase in fragmentation and its market price, but also raises the skilled wage \( p_A \), increases income inequality and induces an apparent skill bias in manufacturing, if the business service sector is included. In contrast to the usual Heckscher-Ohlin logic, a relative increase in the world supply of skilled labor \( \omega < 1 \) could lead to an increase in its relative wage and an increase in relative manufacturing employment, even though manufacturing uses skilled labor less intensively than business services.

4.3. The Effects of an Enlarged Trading Area: Free Entry

In the long run, the existence of economic profits or losses induces entry or exit from the industry. Log-differentiating the system of equations (17), (18), (19) we obtain the following system, in matrix form, setting \( \dot{A} = 0 \):

\[
\begin{bmatrix}
-\frac{(1-\lambda_{L,P})}{\lambda_{L,P}} & \frac{(1-\lambda_{H,P})}{\lambda_{H,P}} & -\sigma \\
\sigma + \frac{(1-\lambda_{L,P})}{\lambda_{L,P}} [\theta_{H,P} + (1-\theta_{H,P})\sigma] & -1 & (1-\theta_{H,P}) \frac{(1-\lambda_{H,P})}{\lambda_{H,P}} & 0 \\
& & & & -1 & -1 & 0 & 0 \\
\end{bmatrix}
\begin{bmatrix}
\dot{L}_S \\
\dot{H}_S \\
\dot{\nu}_Z \\
\end{bmatrix}
= \begin{bmatrix}
\left( \omega \hat{\nu}_{H,P} - \lambda_{L,P} \right) \\
\frac{(1-\theta_{H,P})}{\lambda_{L,P}} [\theta_{H,P} - (1-\theta_{H,P})] \hat{\nu}_{H,P} \\
\frac{\lambda_{L,P} \theta_{H,P} (\sigma - 1) + [(1-\theta_{H,P})\sigma + \theta_{H,P}] k \hat{\nu}_{H,P}}{\lambda_{L,P} \lambda_{H,P}} \\
\end{bmatrix}
\]

Again we can calculate equilibrium changes of our three central variables. Note that the determinant of the matrix in (29), \( \Delta_f \), is now given by

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21 This result is in line with empirical evidence on the impact of trade on productivity (see Cortes/Jean (1997)). For a model in which technology can cause trade and widening skill differentials see Burda/Dluhosch (1999).
\[
\Delta_F = -\frac{\sigma}{\lambda_{HP}^*\lambda_{LP}} \left\{ (1-\lambda_{LP})(1-\lambda_{HP}) + \sigma \theta_{HP}(1-\lambda_{HP})\lambda_{LP} + (1-\theta_{HP})(1-\lambda_{HP})\lambda_{LP} \right\}
\]

which is unambiguously negative.

**Skilled and Unskilled Services Employment**

With free entry of firms in manufacturing, the evolution of employment of low-skilled workers in services \( \hat{L}_S \) is given by:

\[
\hat{L}_S = -\frac{\alpha(1-\lambda_{HP}) + \lambda_{LP}\theta_{HP}(\sigma-1) + \theta_{HP}(1-\theta_{HP})\sigma \hat{\omega}_{HP}}{\lambda_{LP}\lambda_{HP}\Delta_F} \hat{F}
\]

which differs from the short run (no-entry) outcome only due to different values \( \Delta \) in the denominator. Since the determinant is larger in the free entry case, the increase in consumer services is unambiguously smaller in the long run than in the short run.

The effect of an increase in factor endowments on the employment of skilled labor in business services (\( \hat{H}_S \)) has the same sign as the resulting change in total fragmentation (since \( \dot{Z} = \hat{H}_S \), and can be derived as

\[
\dot{H}_S = -\frac{\sigma}{\lambda_{LP}^*\lambda_{HP}\Delta_F} \left[ (1-\lambda_{LP}) + \lambda_{LP}\sigma + (\lambda_{LP} - \omega \hat{\omega}_{HP})(1-\theta_{HP})(1-\sigma) \right] \hat{F}
\]

For an enlargement of the trading area to induce an increase in aggregate business services employment and output, it is sufficient that \( (\lambda_{LP} - \omega \hat{\omega}_{HP})(1-\sigma) > 0 \). Given \( \Delta_F < 0 \), a necessary and sufficient condition on \( \sigma \) is\(^{22}\)

\[
\sigma > \frac{\lambda_{LP}\theta_{HP} + \omega \hat{\omega}_{HP}(1-\theta_{HP}) - 1}{\lambda_{LP}\theta_{HP} + \omega \hat{\omega}_{HP}(1-\theta_{HP})} = 1 - \frac{1}{\lambda_{LP}\theta_{HP} + \omega \hat{\omega}_{HP}(1-\theta_{HP})}
\]

which is strictly less than unity.

\(^{22}\) The analogous condition on \( \omega \): \( \omega < \frac{1-(1-\sigma)\lambda_{LP}\theta_{HP}}{\lambda_{HP}(1-\theta_{HP})} \).
A comparison of necessary and sufficient conditions for no-entry ($S<1$) versus free-entry versions ($S=1$) of the model is illuminating. For growth in business services employment in the short run, it is sufficient for 

$$\sigma > 1 - \frac{\lambda_{L,P}S + (1-S)\omega\lambda_{H,P} + (1-\lambda_{L,P})}{\lambda_{L,P}\theta_{H,P} + (1-\theta_{H,P})\omega\lambda_{H,P}}$$

so the restriction is stricter in the long run if 

$$\lambda_{L,P}S + (1-S)\omega\lambda_{H,P} + (1-\lambda_{L,P}) > 1 \quad \text{or} \quad \omega > \frac{\lambda_{L,P}}{\lambda_{H,P}}.$$

If the relative increase in endowments exceeds the ratio of low- to high-skilled employees in direct manufacturing, Put somewhat differently, the sign of $\frac{\partial H_s}{\partial S}$ in the no-entry case has the same the sign as $\omega\lambda_{H,P} - \lambda_{L,P}$.

To summarize the effects of the market size on employment: an increase in factor endowments expands unskilled service employment if the endowment of low skilled workers increases sufficiently. The interval of $\sigma$ for which both $L_s$ and $H_s$ increase under free entry is given by the interval 

$$\left[ \max \left( 1 - \frac{\min(\omega,1)}{\lambda_{L,P}\theta_{H,P} + (1-\theta_{H,P})\omega\lambda_{H,P}}, 0 \right), \infty \right],$$

which includes the Cobb-Douglas case, and if $\omega$ is not too small, also includes econometric estimates for the manufacturing sector as well (see Hamermesh (1993)).

**Market Price of Business Services and Fragmentation**

The relative price of business services $p_Z$ – the price of coordinating fragmented production processes – is a central variable of interest. If $p_Z$ declines in the long run, then the representative firm will have a larger scale of production and be more globalized:

$$\hat{p}_z = -\frac{(\omega - 1)}{\lambda_{L,P}\lambda_{H,P}\Delta_F} \hat{\theta}_{H/P}$$

(33)

Thus in the long run a necessary and sufficient condition for an increase in firm-level fragmentation is $\omega < 1$. If $\omega > 1$, the long run is characterized by an increase in the price of and a decrease in the extent of fragmentation.
Since the variables in the differentiated goods sector depend only on \( \hat{\rho}_2 \), it follows directly from (16c) that fragmentation in the long run may be fundamentally different from the short run. In particular, firm-level fragmentation will rise with free entry if and only if growth in the endowment of low skilled workers is outstripped by that of high skilled workers. In the short run, in contrast, fragmentation may occur with an increase in wage inequality as well as an increase in skill intensity in manufacturing. From (26) and (33) one could easily imagine a situation in which a uniform expansion of the trading area initially induces an increase in business services employment and fragmentation as well as wage inequality, all of which are reversed as new firms enter the market.

5. Conclusions

The objectives of this paper were two-fold: first, to model general equilibrium implications of cost competition and fragmentation in a monopolistic competition environment, and second, to determine whether trade could explain recent global trends in fragmentation and apparent skill bias in domestic labor markets. In the model studied here, trade and fragmentation are driven by the size of the market. Increased openness puts pressure on firms to cut costs, and as different production techniques are associated with different cost structures, firms in fact compete by choice of production method. The result may be a finer vertical division of labor and outsourcing similar to that observed in the process of globalization.

In our analysis, the impact on fragmentation depends crucially on the time horizon under consideration. When the number of firms is constant, the removal of barriers to trade and mobility induces firms to use more fragmented production structures. This is because total value added increases endogenously by more than the market price for business services. If the expansion of the trading area is biased sufficiently towards unskilled labor, the process of globalization of production may be associated with bimodal growth in high- and low-skilled employment in services. In stressing cost competition, we offer a potential trade
explanation for labor market developments which differs from the traditional account of the
Heckscher-Ohlin-Samuelson model. Globalization implies a shift in relative labor demand
which can reverse the usual effects implied by the Rybczynski Theorem. In a long-run
perspective characterized by free entry, however, these can be either reversed or intensified,
depending on the relative change in factor supplies. In any case, our model may be interpreted
as providing reasons why fragmentation can occur even when factor prices are equalized.23

The model lends itself to a number of extensions, including a more thorough
investigation of the effect of trade on wages.24 A role for diminishing returns in services was
ruled out in this paper, yet may be an aggravating factor in creating income inequality.
Overall, the possibility that technological change in the process of globalization is in part
induced may explain why trade and technology are empirically difficult to disentangle in their
contribution to the immizeration of low-skilled labor in industrialized countries. A
comparison of the consequences of expanding trade with those of exogenous technical change
is an obvious extension, on which we have already reported preliminary results
(Burda/Dluhosch (1999)).

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23 We are grateful to an anonymous referee for suggesting this point.
24 See, for example, the 1997 Symposium in the Journal of Economic Perspectives and the references therein.


